

2023 Canadian Computing Olympiad
Day 1, Problem 1
Binaria

Time Limit: 1 second

Problem Description

You have been hired by the Cheap Communication Organization (CCO) to work on a communication breakthrough: sub-message sum (SMS). This revolutionary idea works as follows.

Given a binary string of length N , and some positive integer K with $K \leq N$, the SMS for the string consists of a sequence of $N - K + 1$ sums. The first sum in the sequence is the sum of digits 1 through K , the second sum is the sum of digits 2 through $K + 1$, and so on until the last sum which is the sum of digits $N - K + 1$ through N .

For example, if $K = 4$, the SMS of the binary string 110010 is 2,2,1. This is because $1 + 1 + 0 + 0 = 2$, $1 + 0 + 0 + 1 = 2$, and $0 + 0 + 1 + 0 = 1$.

Since you are a very junior developer, your job is not to find the original binary string from a given SMS, but rather the number of binary strings that could have formed this SMS.

Input Specification

The first line of input contains the two space-separated integers N and K where $1 \leq K \leq N$.

The second line of input contains $N - K + 1$ space-separated integers which is the SMS of at least one binary string.

Marks Awarded	Bounds on N	Additional Bounds on K
3 marks	$1 \leq N \leq 10$	$K \leq 3$
3 marks	$1 \leq N \leq 10$	None
4 marks	$1 \leq N \leq 1\,000$	$K \leq 10$
4 marks	$1 \leq N \leq 10^6$	$K \leq 20$
4 marks	$1 \leq N \leq 10^6$	$K \leq 3\,000$
7 marks	$1 \leq N \leq 10^6$	None

Output Specification

Output the remainder of T divided by the prime number $10^6 + 3$ where T is the positive integer equal to the total number of possible binary strings that correspond to the given SMS.

Sample Input

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7 4
3 2 2 2
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Output for Sample Input

3

Explanation of Output for Sample Input

The possible strings of length 7 are 1011001, 1101010, and 1110011.