



## Bubble Sort Machine

JOI-kun, an algorithm researcher, has developed a machine called the Bubble Sort Machine.

The Bubble Sort Machine operates on an integer sequence  $a = (a_1, a_2, \dots, a_N)$  of length  $N$ . To activate the Bubble Sort Machine, the initial values  $A_i$  are provided as input for each  $a_i$  ( $1 \leq i \leq N$ ). Each time **Button 1** on the Bubble Sort Machine is pressed, the machine modifies the sequence  $a$  in the following way:

For each  $i = 1, 2, \dots, N - 1$  in order, if  $a_i > a_{i+1}$ , then the values of  $a_i$  and  $a_{i+1}$  are swapped.

To make the Bubble Sort Machine even more appealing, JOI-kun decided to add the following feature:

When **Button 2** is pressed and integers  $l$  and  $r$  satisfying  $1 \leq l \leq r \leq N$  are given as input, the machine outputs the value of  $a_l + a_{l+1} + \dots + a_r$ .

Given the initial values of the integer sequence and the sequence of operations on the Bubble Sort Machine, write a program that computes the outputs produced by Button 2.

### Input

Read the following data from the standard input.

$N$   
 $A_1 A_2 \dots A_N$   
 $Q$   
(Query 1)  
(Query 2)  
 $\vdots$   
(Query  $Q$ )

Here,  $Q$  is the number of operations performed on the Bubble Sort Machine. Each (Query  $j$ ) ( $1 \leq j \leq Q$ ) consists space separated integers. Let  $T_j$  denote the first integer of (Query  $j$ ). The content of this line is one of the following.

- If  $T_j = 1$ , this line contains no additional integers. This means that the  $j$ -th operation on the Bubble Sort Machine is pressing Button 1.
- If  $T_j = 2$ , this line contains two more integers,  $L_j$  and  $R_j$ , in that order. This means that the  $j$ -th operation on the Bubble Sort Machine is pressing Button 2 with the integers  $L_j$  and  $R_j$  as input.



## Output

For each operation where Button 2 is pressed, that is, for each  $j$  ( $1 \leq j \leq Q$ ) such that  $T_j = 2$ , output the integer produced by the Bubble Sort Machine on a separate line in the order of the queries.

## Constraints

- $2 \leq N \leq 500\,000$ .
- $1 \leq A_i \leq 10^9$  ( $1 \leq i \leq N$ ).
- $1 \leq Q \leq 500\,000$ .
- $T_j$  is either 1 or 2 ( $1 \leq j \leq Q$ ).
- If  $T_j = 2$ ,  $1 \leq L_j \leq R_j \leq N$  ( $1 \leq j \leq Q$ ).
- Given values are all integers.

## Subtasks

1. (5 points) The number of  $j$  ( $1 \leq j \leq Q$ ) such that  $T_j = 1$  is at most 10.
2. (11 points)  $N \leq 150\,000$ ,  $Q \leq 150\,000$ ,  $L_j = R_j = 1$  if  $T_j = 2$  ( $1 \leq j \leq Q$ ).
3. (15 points)  $N \leq 150\,000$ ,  $Q \leq 150\,000$ ,  $1 \leq A_i \leq 2$  ( $1 \leq i \leq N$ ).
4. (23 points)  $N \leq 150\,000$ ,  $Q \leq 150\,000$ ,  $L_j = R_j$  if  $T_j = 2$  ( $1 \leq j \leq Q$ ).
5. (29 points)  $N \leq 150\,000$ ,  $Q \leq 150\,000$ .
6. (17 points) No additional constraints.



## Sample Input and Output

| Sample Input 1 | Sample Output 1 |
|----------------|-----------------|
| 4              | 13              |
| 5 3 5 2        | 3               |
| 6              | 12              |
| 2 1 3          | 5               |
| 1              |                 |
| 2 1 1          |                 |
| 2 2 4          |                 |
| 1              |                 |
| 2 1 2          |                 |

First, the initial values  $a_1 = 5$ ,  $a_2 = 3$ ,  $a_3 = 5$ , and  $a_4 = 2$  are given, initializing  $a = (5, 3, 5, 2)$ . The operations of the Bubble Sort Machine proceed as follows:

1. Button 2 is pressed with  $l = 1$ ,  $r = 3$  as input. The Bubble Sort Machine outputs  $a_1 + a_2 + a_3 = 13$ .
2. Button 1 is pressed. For  $i = 1, 2, 3$ , the following operations are performed in order:
  - For  $i = 1$ : Since  $a_1 > a_2$  holds, their values are swapped, resulting in  $a = (3, 5, 5, 2)$ .
  - For  $i = 2$ : Since  $a_2 > a_3$  does not hold, no change is made to  $a$ .
  - For  $i = 3$ : Since  $a_3 > a_4$  holds, their values are swapped, resulting in  $a = (3, 5, 2, 5)$ .
3. Button 2 is pressed with  $l = 1$ ,  $r = 1$  as input. The Bubble Sort Machine outputs  $a_1 = 3$ .
4. Button 2 is pressed with  $l = 2$ ,  $r = 4$  as input. The Bubble Sort Machine outputs  $a_2 + a_3 + a_4 = 12$ .
5. Button 1 is pressed. For  $i = 1, 2, 3$ , the following operations are performed in order:
  - For  $i = 1$ : Since  $a_1 > a_2$  does not hold, no change is made to  $a$ .
  - For  $i = 2$ : Since  $a_2 > a_3$  holds, their values are swapped, resulting in  $a = (3, 2, 5, 5)$ .
  - For  $i = 3$ : Since  $a_3 > a_4$  does not hold, no change is made to  $a$ .
6. Button 2 is pressed with  $l = 1$ ,  $r = 2$  as input. The Bubble Sort Machine outputs  $a_1 + a_2 = 5$ .

This sample input satisfies the constraints of subtasks 1, 5, and 6.



| Sample Input 2 | Sample Output 2 |
|----------------|-----------------|
| 5              | 3               |
| 1 1 2 1 2      | 4               |
| 5              | 4               |
| 2 2 3          |                 |
| 1              |                 |
| 2 2 4          |                 |
| 1              |                 |
| 2 2 4          |                 |

This sample input satisfies the constraints of subtasks 1, 3, 5, and 6.