

## Problem D. Xoractive

Time limit: 1 second  
Memory limit: 256 megabytes

Aidos has come up with a puzzle and challenged Temirulan to solve it. He picked a sequence  $a$  of  $n$  non-negative integers numbered from 1 to  $n$ :  $a_1, a_2, \dots, a_n$ .

Temirulan can ask two types of questions:

- *ask* — Reveal the number at position  $i$  of the given sequence.
- *get\_pairwise\_xor* — For the given sequence of distinct integer numbers:  $i_1, i_2, \dots, i_k$ , get a set of pairwise values of *xor* for the elements of the sequence  $a$  at indexes  $i_1, i_2, \dots, i_k$ ,  $\{a_{i_x} \oplus a_{i_y} \mid 1 \leq x, y \leq k\}$ .

For example, let's assume that Aidos has picked the sequence  $[1, 5, 6, 3]$ . Then for the question *ask*(2), Aidos will answer with the number 5 and for the question *get\_pairwise\_xor*( $\{3, 4\}$ ), Aidos will answer with the sequence  $[0, 0, 5, 5]$ , because

- $a_3 \oplus a_4 = 6 \oplus 3 = 5$
- $a_4 \oplus a_3 = 3 \oplus 6 = 5$
- $a_3 \oplus a_3 = 6 \oplus 6 = 0$
- $a_4 \oplus a_4 = 3 \oplus 3 = 0$ .

Temirulan failed to cope with the puzzle and your task is to help him. Find the hidden sequence using the questions described above.

### Interaction Protocol

YOUR SUBMISSIONS MUST NOT READ FROM THE STANDARD INPUT, PRINT TO THE STANDARD OUTPUT OR INTERACT WITH ANY OTHER FILE.

Your task is to implement the following function: `int[] guess(int n)`

- $n$ : the length of the hidden sequence.
- The function is called exactly one time for each test.
- The function has to return the hidden sequence in the same order.

Your function can call the following functions:

1. `int ask(int i)`

- $i$ : index of the number in sequence,  $1 \leq i \leq n$ .
- The function returns the  $i$ -th number of the hidden sequence.

2. `int[] get_pairwise_xor(int[] pos)`

- $pos$ : **non empty** list of indexes of the sequence.
- All of the elements in  $pos$  must be **distinct** integers.
- Let  $k$  be the number of elements in  $pos$ . Then  $1 \leq pos_i \leq n$  for each  $1 \leq i \leq k$ .
- The function returns sorted list of  $k^2$  elements: a set of pairwise values *xor*,  $\{a_{pos_x} \oplus a_{pos_y} \mid 1 \leq x, y \leq k\}$ .

You can call both functions no more than 200 times in total for each test. If any of the above conditions are violated, your program will get **Wrong Answer** verdict. Otherwise, your program will get **Accepted** verdict and your score is calculated based on the total number of calls of the functions *ask* and *get\_pairwise\_xor* (Refer to the section "Scoring").

## Scoring

- $2 \leq n \leq 100$
- $0 \leq a_i \leq 10^9$  for each  $1 \leq i \leq n$ .

In this task, the grader is NOT adaptive. It means that the sequence  $a$  is fixed at the beginning of the running of the grader and does not depend on calls from your program.

1. (6 points)  $n \leq 4$
2. (94 points) No additional constraints. For this subtask, your score is calculated in the following manner. Let  $q$  be the total number of calls of the functions *ask* and *get\_pairwise\_xor*.
  - If  $q \leq 15$ , your score is 94.
  - If  $15 < q \leq 40$ , your score is  $84 - 2(q - 16)$ .
  - If  $40 < q \leq 50$ , your score is 35.
  - Otherwise, your score is 0.

Note that your score for each subtask is the minimum score among all the results on tests of the corresponding subtask.

## Note

The *xor* operation is the bitwise exclusive OR.

Let the hidden sequence  $a$  be  $[1, 5, 6, 3]$ . Grader calls the function. Example of the interaction is below.

Call	Result
<i>ask</i> (2)	5
<i>get_pairwise_xor</i> ({1, 2, 3})	{0, 0, 0, 3, 3, 4, 4, 7, 7}
<i>ask</i> (3)	6
<i>get_pairwise_xor</i> ({4, 2})	{0, 0, 6, 6}
<i>get_pairwise_xor</i> ({2})	{0}

The sample grader reads the input in the following format:

- Line 1:  $n$
- Line 2:  $a_1, a_2, \dots, a_n$

YOU CAN DOWNLOAD `xoractive.zip` in the system that contains examples for languages Java, C++11, FPC, Python 2.

All the examples of calling the functions can be found above. For Python 2, you have to implement the function `def guess(n, interactor)`, where *interactor* is an instance of the class being tested. Functions *ask* and *get\_pairwise\_xor* are the methods of this class.

`xoractive.zip` contains examples of solutions for each language.

For the solutions in Java language, file and class name have to be named as `Xoractive.java` and `Xoractive` respectively.

For the solutions in Pascal language, file has to be named as `xoractive.pas`.