

# Pyramids

Everyone knows that Pharaoh Khufu was a great ruler, but many are unaware that he was also a fashion enthusiast. Back in the day, he had  $N$  pyramids numbered from 0 to  $N - 1$ , with pyramid  $i$  ( $0 \leq i < N$ ) consisting of  $A[i]$  stones. He also had the latest catalogue of the most fashionable pyramids of the year. The catalogue consists of  $N$  pyramids numbered from 0 to  $N - 1$ , with pyramid  $i$  ( $0 \leq i < N$ ) consisting of  $B[i]$  stones.

For any  $x$  and  $y$ , such that  $0 \leq x \leq y < N$ , we define a **range of pyramids**  $A[x..y]$  to be a sequence  $A[x], A[x + 1], \dots, A[y]$ . We also define a range of pyramids  $B[x..y]$  analogously.

Every day, Khufu would browse the catalogue and choose two ranges of pyramids  $A[L..R]$  and  $B[X..Y]$  where  $R - L = Y - X$  (the values of  $L, R, X$  and  $Y$  may be different every day). After that, he would like to know whether it's possible to **transform** his range  $A[L..R]$  to become equal to the catalogue's range  $B[X..Y]$ . Transforming a range consists of performing the following step an arbitrary number of times: take one stone from a pyramid within the range and move it to an adjacent pyramid within the range.

Your task is to answer multiple questions of the following form. Given four integers  $L, R, X$ , and  $Y$ , determine whether it is possible to transform  $A[L..R]$  into  $B[X..Y]$ . Note that **the number of stones in each pyramid never actually changes**, Khufu only wonders if one range **could** be transformed into the other one.

## Implementation Details

You should implement the following procedures:

```
void init(std::vector<int> A, std::vector<int> B)
```

- $A, B$ : two arrays of length  $N$ , describing the number of stones in Khufu's pyramids and in the catalogue respectively.
- This procedure is called exactly once, before any calls to `can_transform`.

```
bool can_transform(int L, int R, int X, int Y)
```

- $L, R$ : starting and ending indices of Khufu's pyramids range.
- $X, Y$ : starting and ending indices of catalogue's pyramids range.
- This procedure should return `true` if it's possible to transform  $A[L..R]$  into  $B[X..Y]$  and `false` otherwise.

- This procedure is called exactly  $Q$  times, once for each day.

## Example

Consider the following call:

```
init([1, 2, 3, 4, 5], [2, 2, 2, 4, 5])
```

Assume the grader then calls `can_transform(0, 2, 0, 2)`. This call should return whether sequence of pyramids  $A[0..2] = [1, 2, 3]$  can be transformed into  $B[0..2] = [2, 2, 2]$ . This is indeed possible by moving 1 stone from the last to the first pyramid in the range. Therefore, this call should return `true`.

Assume the grader then calls `can_transform(3, 4, 3, 4)`. This call should return whether we can transform Khufu's pyramids  $A[3..4] = [4, 5]$  to  $B[3..4] = [4, 5]$  or not. The pyramids already look alike. Therefore, this call should return `true`.

Assume the grader then calls `can_transform(0, 2, 1, 3)`. This call should return whether sequence of pyramids  $A[0..2] = [1, 2, 3]$  can be transformed into  $B[1..3] = [2, 2, 4]$ . This is not possible, and thus this call should return `false`.

## Constraints

- $1 \leq N \leq 100\,000$
- $1 \leq Q \leq 100\,000$
- $1 \leq A[i] \leq 10^9$
- $1 \leq B[i] \leq 10^9$

In each call to `can_transform`:

- $0 \leq L \leq R < N$
- $0 \leq X \leq Y < N$
- $R - L = Y - X$

## Subtasks

Subtask	Score	Additional Constraints
1	10	$N \leq 5$ ; $Q \leq 10$ ; $A[i] \leq 5$ , $B[i] \leq 5$ for each $i$ such that $0 \leq i < N$
2	40	$N \leq 1000$ ; $Q \leq 1000$
3	20	$A[i] \leq 2$ and $B[i] \leq 2$ for each $i$ such that $0 \leq i < N$
4	30	No additional constraints.

## Sample grader

Input format:

```
N Q
A[0] A[1] ... A[N-1]
B[0] B[1] ... B[N-1]
L[0] R[0] X[0] Y[0]
L[1] R[1] X[1] Y[1]
...
L[Q-1] R[Q-1] X[Q-1] Y[Q-1]
```

Here,  $L[i]$ ,  $R[i]$ ,  $X[i]$ , and  $Y[i]$  denote the values of  $L$ ,  $R$ ,  $X$  and  $Y$  in the  $i$ -th call to `can_transform`, respectively.

Output format:

```
P[0]
P[1]
...
P[Q-1]
```

Here,  $P[i]$  is 1 if the  $i$ -th call to `can_transform` returns `true` and 0 otherwise.