



## Naan

JOI Curry Shop is famous for serving very long naans. They have  $L$  kinds of flavours, numbered from 1 to  $L$ , to flavour naans. “JOI Special Naan” is the most popular menu in the shop. The length of the naan is  $L$  cm. We define “point  $x$ ” as the point on the naan which distant  $x$  cm from the left end of the naan. The segment between point  $j - 1$  and point  $j$  are flavoured by flavour  $j$  ( $1 \leq j \leq L$ ).

$N$  people came to JOI Curry Shop. Their preferences are different from other. Specifically, when  $i$  th ( $1 \leq j \leq L$ ) person eat naan with flavour  $j$  ( $1 \leq j \leq L$ ), she will get  $V_{i,j}$  happiness per 1 cm.

They ordered only one JOI Special Naan. They will share the naan in the following manner:

1. Choose  $N - 1$  fractions  $X_1, \dots, X_{N-1}$ , which satisfies  $0 < X_1 < X_2 < \dots < X_{N-1} < L$ .
2. Choose  $N$  integers  $P_1, \dots, P_N$ . This have to be a permutation of  $1, \dots, N$ .
3. For each  $k$  ( $1 \leq k \leq N - 1$ ), cut the naan at point  $X_k$ . Thus, naan will be separated into  $N$  pieces.
4. For each  $k$  ( $1 \leq k \leq N$ ), give the piece between point  $X_{k-1}$  and point  $X_k$ . We consider  $X_0$  as 0 and  $X_N$  as  $L$ .

We want to distribute the naan fairly. We say a distribution is **fair** if each person get more than or equal to one  $N$  th amount of happiness compared to the amount of happiness she will get when she eat whole JOI Special Naan.

Given the information of preferences of  $N$  people, determine if it is possible to distribute the naan in a fair way. If it is possible, output the way you distribute the naan in a fair way.

## Input

Input data will be given in the following form. All values in input are integer.

```
N L
V1,1 V1,2 ⋯ V1,L
⋮
VN,1 VN,2 ⋯ VN,L
```

## Output

If it is impossible to distribute naan in a fair way, output -1 in a line. If it is possible, output  $N - 1$  fractions  $X_1, \dots, X_{N-1}$  and  $N$  integers  $P_1, \dots, P_N$  that represent a fair distribution, in the following format.



$$\begin{array}{l} A_1 B_1 \\ A_2 B_2 \\ \vdots \\ A_{N-1} B_{N-1} \\ P_1 P_2 \cdots P_N \end{array}$$

$A_i, B_i$  are the pair of integers that satisfies  $X_i = \frac{A_i}{B_i} (1 \leq i \leq N)$ . These integers have to follow “Constraints of Output”.

## Constraints of Input

- $1 \leq N \leq 2\,000$ .
- $1 \leq L \leq 2\,000$ .
- $1 \leq V_{i,j} \leq 100\,000 (1 \leq i \leq N, 1 \leq j \leq L)$ .

## Constraints of Output

If it is possible to distribute the naan in a fair way, the output must satisfy the following constraints:

- $1 \leq B_i \leq 1\,000\,000\,000 (1 \leq i \leq N)$ .
- $0 < \frac{A_1}{B_1} < \frac{A_2}{B_2} < \cdots < \frac{A_{N-1}}{B_{N-1}} < L$ .
- $P_1, \dots, P_N$  is a permutation of  $1, \dots, N$ .
- In the distribution, the amount of happiness that  $i$  th person will get is more than or equal to  $\frac{V_{i,1} + V_{i,2} + \cdots + V_{i,L}}{N} (1 \leq i \leq N)$ .

$A_i$  and  $B_i$  are **not** necessary to be coprime.

Under the constraints of input, it can be proved that if fair distribution exists, there is a correct output that satisfies  $1 \leq B_i \leq 1\,000\,000\,000 (1 \leq i \leq N)$ .

## Subtask

1. (5 points)  $N = 2$ .
2. (24 points)  $N \leq 6, V_{i,j} \leq 10 (1 \leq i \leq N, 1 \leq j \leq L)$ .
3. (71 points) There are no additional constraints.



## Sample Input and Output

Sample Input 1	Sample Output 1
2 5	14 5
2 7 1 8 2	2 1
3 1 4 1 5	

In this sample, the first person will get  $2 + 7 + 1 + 8 + 2 = 20$  happiness when she eat whole naan and the second person will get  $3 + 1 + 4 + 1 + 5 = 14$  happiness when she eat whole naan. Thus, if the first person get happiness more than or equal to  $\frac{20}{2} = 10$  and the second person get happiness more than or equal to  $\frac{14}{2} = 7$ , the distribution is fair.

If you cut the naan at point  $\frac{14}{5}$ , the first person will get  $1 \times \frac{1}{5} + 8 + 2 = \frac{51}{5}$  happiness and the second person will get  $3 + 1 + 4 \times \frac{4}{5} = \frac{36}{5}$  happiness. Hence, this is a fair distribution.

Sample Input 2	Sample Output 2
7 1	1 7
1	2 7
2	3 7
3	4 7
4	5 7
5	6 7
6	3 1 4 2 7 6 5
7	

In this sample, the naan has only one flavour. If you equally divide the naan into 7 pieces, the distribution will be fair, regardless of  $P_1, \dots, P_N$ .

Sample Input 3	Sample Output 3
5 3	15 28
2 3 1	35 28
1 1 1	50 28
2 2 1	70 28
1 2 2	3 1 5 2 4
1 2 1	



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Note that  $A_i$  and  $B_i$  are not necessary to be coprime ( $1 \leq i \leq N$ ).