

### Lithuanian Olympiad in Informatics

Final Round • Nemenčinė, 2019 March 30th-31st • Senior Division mokesciai-vyr

## Tax Evasion

Just, Inc. is a huge international company that owns N bank accounts in various countries. The accounts are linked by N-1 direct channels such that it is possible to transfer money from any account to any other account either directly or through intermediate accounts.

If two accounts are linked by a direct channel, a transfer takes an evening to complete. If there is no direct channel, the transfer will involve intermediate accounts and thus it will take multiple days for funds to reach their destination.



*External Revenue Service (ERS)* suspects that *Just* is evading taxes, therefore it plans to investigate all the accounts that belong to the company. The investigation will be performed as follows:

- 1. On the morning of the first day, ERS will investigate the account No. 1:
  - If there is 1 gigadollar in the account, *Just* will immediately have to pay taxes.
  - If there are 2 or more gigadollars, the CEO will be charged with forgery and imprisoned. There is no way *Just* would allow for this to happen.
  - If the account is empty, *Just* will not yet have to pay taxes after the investigation of this account.
- 2. On the evening of the first day, *Just* will send a non-negative integer amount of gigadollars through each of the channels in either direction. However, *Just* cannot transfer money to or from the account which was investigated earlier on the same day (i.e. No. 1).
- 3. On the morning of the second day, ERS will investigate one of the accounts that is linked via a direct channel with the previously investigated account No. 1. The account is processed in the same way as described above. Just has no idea as to which account ERS will choose.
- 4. On the evening of the second day, *Just* will make new transfers. As before, the account which was just investigated cannot be used.
- 5. The investigations of accounts will continue on the third and further days until ERS decides that it has performed enough investigations.

Just is well aware of the investigation procedure. It plans on transferring money between accounts every day in such a way that the money would not be detected for as long as possible and that the company would never be charged with forgery. However, Just does not know which accounts ERS will be choosing and how many investigations will take place, so it must prepare for the **worst possible scenario**. In other words, Just will transfer money in such a way that no matter what ERS does, the company will not be charged with forgery and will postpone paying taxes the first time as far as possible.

# Lithuanian Olympiad in Informatics Final Round • Nemenčinė, 2019 March 30th-31st • Senior Division mokesciai-vyr

**Task.** On the morning of the first day there is 1 gig adollar in M different accounts. The rest of the accounts are empty.

Write a program that finds the earliest day on which *Just* will have to pay taxes for the first time, assuming it transfer money between accounts in an optimal way.

**Input.** The first line contains two integers N (number of accounts) and M (number of accounts that contain 1 gigadollar at the beginning).

The next N-1 lines contain integers  $s_1, s_2, ..., s_{N-1}$  (one integer per line).  $s_i$   $(1 \le s_i \le i)$  denotes that there is a direct channel between accounts (i+1) and  $s_i$ .

The last line contains M distinct integers – the list of account numbers that have one gigadollar at the beggining.

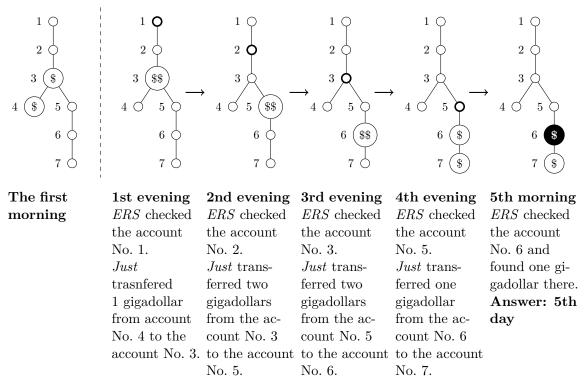
**Output.** Output one integer – the number of day when *Just* will have to pay the taxes for the first time.

Input	Output	Comment
7 2	5	The worst case is illiustrated in the first
1		picture.
2		If, however, on the fourth evening <i>Just</i> had
3		sent two gigadollars to the account No.
3		7, on the fifth morning $ERS$ would have
5		found the sixth account empty, but on the
6		sixth day would have found an account with
3 4		two gigadollars and <i>Just</i> would have been
		charged with forgery.

#### Examples.



Final Round • Nemenčinė, 2019 March 30th-31st • Senior Division mokesciai-vyr



 $Figure \ 1 \ Il liustration \ of \ the \ first \ example$ 

Input	Output	Comment
11 3	5	If Just sent one gigadollar from the ac-
1		count No. 5 to the account No. 3, money
2		would reach the destination account only
3		in the evening of the second day. However,
4		on the third morning $ERS$ would check
3		the account No. 3 and find this money, so
6		Just will leave one gigadollar in the account
7		No. 5, and $ERS$ will find it on the morning
8		of the fifth day.
9		
10		
345		
		3 (\$)
		4 (\$) 6
		5 (\$) 0 7
		Q 8
		0 9
		O 10
		O 11
	Page 3 of 4	



## Lithuanian Olympiad in Informatics

Final Round • Nemenčinė, 2019 March 30th-31st • Senior Division mokesciai-vyr

Input	Output	Comment
4 3	2	If Just tried to postpone taxes on the sec-
1		ond morning, it will be charged with forgery
2		later on (look at Figure $2$ ).
3		
234		
L	1	

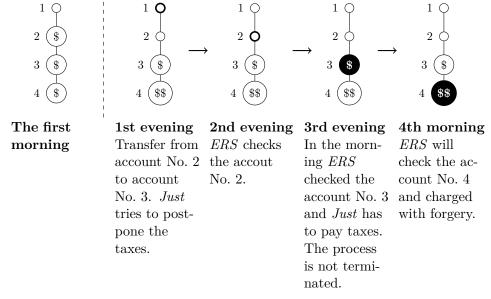


Figure 2 Illustration of the third example. Bad Just strategy.

**Subtasks.** For all tests:  $1 \le N \le 200\,000, 1 \le M \le N$ .

No.	Points	Additional constraints
1	10	$s_i = i$
2	22	M = 1
3	39	$N \le 5000$
4	29	No additional constraints